Haskell for Readers

Joachim Breitner, DFINITY Foundation⁺

Exercise 1

What associativity do you expect for (+) and (-)? Verify your expectation.

Exercise 2

Look up the precedences of the other arithmetic operations, and see how that corresponds to the PEMDAS rule.

Exercise 3

Can you predict the result of the following?

Prelude> 1 + const 2 3 + 4

Exercise 4

What is the result of

Prelude> (-) 5 \$ div 16 \$ (-) 10 \$ 4 `div` 2

Exercise 5

Discuss: Think of other programming language that have concepts called functions. Can you always replace a function call with the function definition? Does it change the meaning of the program?

Exercise 6

Write a function absoluteValue with one parameter. If the parameter is negative, returns its opposite number, otherwise the number itself.

Exercise 7

Write a function isHalfRound that checks if a number is divisible by 5, by checking whether the last digit is 0 or 5.

Exercise 8

Write a function isEven that checks if a number is divisible by 2, by checking whether the last digit is 0, 2, 4, 6, 8.

Exercise 9

Write the function sumDigits that sums up the digits of a natural number.

Exercise 10

^{*}http://www.joachim-breitner.de/

[†]https://dfinity.org/

Write a (recursive) function fixEq so that fixEq f x repeatedly applies f to x until the result of f is the same as its argument.

Exercise 11

Use this function and sumDigits to write a function isMultipleOf3 so that isMultipleOf3 x is true if repeatedly applying sumDigits to x results in 3, 6 or 9.

Exercise 12

Which other recent definitions can be changed accordingly?

Exercise 13

What do you think is the type of id?

Exercise 14

A great example for the power of polymorphism is the following type signature:

(a -> b -> c) -> b -> a -> c

There is a function of that type in the standard library. Can you tell what it does? Can you guess its name? You can use a type-based search engine like Hoogle¹ or Hayoo² to find the function.

Exercise 15

Consider the following definition:

data Wat = Wat Wat

Is this legal? What does it mean? Which occurrences of Wat are terms, and which are types? Can you define a value of type Wat?

Exercise 16

How many values are there of type Maybe (Maybe Bool). When can it be useful to nest Maybe in that way?

Exercise 17

How could you represent the Riemann numbers from the previous section using only these predefined data types?

Exercise 18

Write functions

```
fromEitherUnit :: Either () a -> Maybe a
```

and

toEitherUnit :: Maybe a -> Either () a

that are inverses to each other.

In only one of these type signatures you can replace () with a new type variable b, and still implement the function. In which one? Why?

¹https://www.haskell.org/hoogle/?hoogle=%28a+-%3E+b+-%3E+c%29+-%3E+b+-%3E+a+-%3E+c ²http://hayoo.fh-wedel.de/?query=%28a+-%3E+b+-%3E+c%29+-%3E+b+-%3E+a+-%3E+c

Exercise 19

What does this program print?

```
theAnswer :: IO Integer
theAnswer = do
  putStrLn "Pondering the question..."
  return 23
  return 42
main :: IO ()
main = do
  a <- theAnswer
  putStrLn (show a)
Exercise 20
```

What does this program do?

Exercise 21

Write an Eq instance for Employee, using record accessors. Is there a problem with this code?

Exercise 22

Look up the Semigroup type class, and find its laws.

Exercise 23

Can you think of a Semigroup (Tree a) instance? Or maybe even more than one? How can you be sure it is a lawful instance?

Exercise 24

The Monoid class³ extends the Semigroup class with an operation mempty :: Monoid a => a that is supposed to be a neutral element of (<>).

Given a function signature summarize :: Monoid a => Tree a -> a, can you guess what it does? What would be the implementation you expect?

³http://hackage.haskell.org/package/base/docs/Prelude.html#t:Monoid

With that implementation, can you use summarize to distinguish trees that differ in shape, but have the same elements in the same order? What does this imply for search trees?

Exercise 27

Implement for M :: Monad $m \Rightarrow [a] \rightarrow (a \rightarrow m b) \rightarrow m [b]$ using do-notation.

Exercise 25

Give definitions of the operators up to join using (>>=), return, and operators you already defined. (You will have to change the constraints to Monad for this to typecheck.)

Exercise 26

Why is the type not when :: Bool -> m a -> m a?

Exercise 28

You might observe that Tagged is simply the existing pair type. There is an Applicative instance for pairs. Look it up! How does that fit to what I just said?